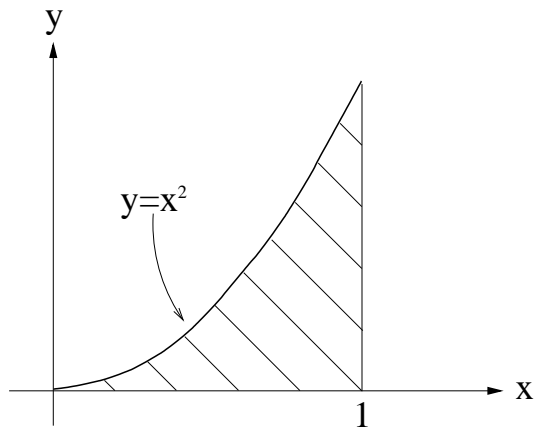


Question

Sketch the region enclosed by the given curves and find the volume of the solid generated when it is revolved about the x -axis:

$$y = x^2, x = 1, y = 0.$$

Answer

Use the disc method:

$$\int_{x=0}^{x=1} \pi(x^2)^2 dx = \pi \int_{x=0}^{x=1} x^4 dx = \pi \left[\frac{x^5}{5} \right]_0^1 = \frac{\pi}{5}$$