Question

Check the Henon map is invertible when $b \neq 0$; find a formula for its inverse.

Answer

If
$$X = a - x^2 + by$$
, $Y = x$ then $x = Y$ and $y = b^{-1}(X - a + Y^2)$: so the inverse map to f is $(X, Y) \mapsto (Y, b^{-1}(X - a + Y^2))$.