

Question

Find the fixed, or invariant points of the Möbius transformation

$$w = \frac{(2z - 5)}{(z + 4)}.$$

Answer

We require points $z \xrightarrow{w=f(z)} z$

$$\text{Thus } z = \frac{(2z - 5)}{(z + 4)}$$

$$\Rightarrow z^2 + 2z + 5 = 0 \Rightarrow z = -1 \pm 2i$$