Exam Question

Topic: Double Integral

T is the triangle in the x-y plane with vertices (0,0), (0,3), (1,3).

Evaluate the integral

$$\iint_T 6\exp(-y^2) \, d(x,y).$$

Express your answer in terms of e, and also as an approximation correct to 6 decimal places using your calculator.

Solution

The correct choice of order of integration has to be made. It can't be done the other way round

$$I = \int_0^3 dy \int_0^{y/3} 6 \exp(-y^2) dx = \int_0^3 2y \exp(-y^2) dy$$
$$= \left[-exp \left(-y^2 \right) \right]_0^3 = 1 - e^{-9} = 0.99877 \quad (6 \text{ d.p.})$$