

Multiple Integration
Iteration of Double Integrals

Question

Calculate the given iterated integral.

$$\int_0^2 dy \int_0^y y^2 e^{xy} dx$$

Answer

$$\begin{aligned} & \int_0^2 dy \int_0^y y^2 e^{xy} dx \\ &= \int_0^2 y^2 dy \left(\frac{1}{y} e^{xy} \Big|_{x=0}^{x=y} \right) \\ &= \int_0^2 y (e^{y^2} - 1) dy = \frac{e^{y^2} - y^2}{2} \Big|_0^2 \\ &= \frac{e^4 - 5}{2} \end{aligned}$$