

Multiple Integration
Iteration of Double Integrals

Question

Calculate the given iterated integral.

$$\int_0^{\pi} \int_{-x}^x \cos y \, dy \, dx$$

Answer

$$\begin{aligned} & \int_0^{\pi} \int_{-x}^x \cos y \, dy \, dx \\ &= \int_0^{\pi} \sin y \Big|_{y=-x}^{y=x} \, dx \\ &= 2 \int_0^{\pi} \sin x \, dx = -2 \cos x \Big|_0^{\pi} \\ &= 4 \end{aligned}$$