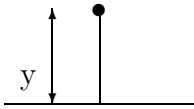


Question

A rubber ball is dropped from rest onto a tile floor a distance h_1 away. The ball bounces up to a height h_2 . What is the coefficient of restitution?

Answer

The ball falls under gravity:



By Newton's 2nd law:

$$\begin{aligned}m\ddot{y} &= -mg \\mv \frac{dv}{dy} &= -mg \quad (v = \dot{y}) \\ \frac{1}{2}v^2 &= -gy + gh_1\end{aligned}$$

Hence on impact with the floor $v = v_0 = \sqrt{2gh_1}$

Also if the ball has speed v_1 (upwards) just after impact, $v_1 = \sqrt{2gh_2}$

Now by differentiation $v_1 = ev_0 \Rightarrow e = \frac{v_1}{v_0} = \sqrt{\frac{h_2}{h_1}}$