

QUESTION

Find the eigenvalues of the rotation matrix

$$A = \begin{bmatrix} \cos \theta & -\sin \theta \\ \sin \theta & \cos \theta \end{bmatrix}.$$

ANSWER

The eigenvalues are  $\cos \theta \pm i \sin \theta = e^{\pm i\theta}$ .