

QUESTION

If $\mathbf{a} = \mathbf{j} + \mathbf{k}$ and $\mathbf{b} = 2\mathbf{i} - \mathbf{j} + 2\mathbf{k}$ find the component of \mathbf{a} in the direction of \mathbf{b} .

ANSWER

$\mathbf{a} = (0, 1, 1)$, $\mathbf{b} = (2, -1, 2)$

The component of \mathbf{a} in the direction of \mathbf{b} is $\mathbf{a} \cdot \hat{\mathbf{b}}$

$$\begin{aligned}\mathbf{a} \cdot \hat{\mathbf{b}} &= (0, 1, 1) \frac{(2, -1, 2)}{\sqrt{2^2 + (-1)^2 + 2^2}} \\ &= \frac{1}{3}(0, 1, 1) \cdot (2, -1, 2) \\ &= \frac{1}{3}(0 - 1 + 2) = \frac{1}{3}\end{aligned}$$