

Vector Functions and Curves
One variable functions

Question

Find the velocity, speed and acceleration of the particle with position given by $\underline{r}(t)$ at time t . Also determine the particles path.

$$\underline{r} = a \cos \omega t \underline{i} + b \underline{j} + a \sin \omega t \underline{k}$$

Answer

Position: $\underline{r} = a \cos \omega t \underline{i} + b \underline{j} + a \sin \omega t \underline{k}$

Velocity: $\underline{v} = -a\omega \sin \omega t \underline{i} + a\omega \cos \omega t \underline{k}$

Speed: $v = |a\omega|$

Acceleration: $\underline{a} = -a\omega^2 \cos \omega t \underline{i} - a\omega^2 \sin \omega t \underline{k}$

Path: the circle $x^2 + z^2 = a^2$, $y = b$.