

**Question**

A force of 2 units acts through the point Q (1, 2, 0), in the direction of the vector (3, 4, -1). Find its moment about the point A (2, 2, -2).

**Answer**

$$\mathbf{M} = \mathbf{r} \times \mathbf{F}$$

$$\mathbf{r} = \vec{AQ} = \vec{OQ} - \vec{OA} = (1, 2, 0) - (2, 2, -2) = (-1, 0, 2)$$

$$\mathbf{F} = 2\hat{\mathbf{F}} \text{ (unit vector in direction of } \mathbf{F}\text{)}$$

$$\mathbf{M} = \mathbf{r} \times \mathbf{F} = \mathbf{r} \times (2\hat{\mathbf{F}}) = 2\mathbf{r} \times \hat{\mathbf{F}}$$

$$\hat{\mathbf{F}} = \frac{(3,4,1)}{\sqrt{3^2+4^2+(-1)^2}} = \left( \frac{3}{\sqrt{26}}, \frac{4}{\sqrt{26}}, \frac{-1}{\sqrt{26}} \right)$$

$$\mathbf{r} \times \hat{\mathbf{F}} = \left\{ \frac{-8}{\sqrt{26}}, \frac{5}{\sqrt{26}}, \frac{-4}{\sqrt{26}} \right\}$$

$$\mathbf{M} = \mathbf{r} \times \mathbf{F} = \left( \frac{-16}{\sqrt{26}}, \frac{10}{\sqrt{26}}, \frac{-8}{\sqrt{26}} \right)$$