

Question

Prove that

$$16 \cos^4 \theta \sin \theta = \sin 5\theta + 3 \sin 3\theta + 2 \sin \theta$$

Answer

Use $\sin 5\theta + 3 \sin 3\theta + 2 \sin \theta = \text{Im}\{(c + is)^5 + 3(c + is)^3 + 2(c + is)\}$

Expand and take imaginary parts, using the fact that $c^2 + s^2 = 1$