

**Applications of Partial Differentiation**  
*Extremes within restricted domains*

**Question**

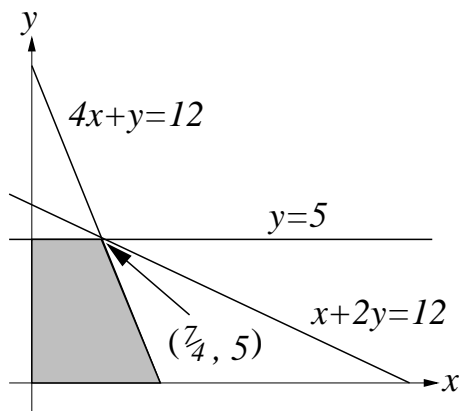
$$Q(x, y) = 2x + 3y$$

Maximize  $Q$ , subject to

$$\begin{aligned}x &\geq 0 \\y &\geq 0 \\y &\leq 5 \\x + 2y &\leq 12 \\4x + y &\leq 12\end{aligned}$$

**Answer**

Maximize  $Q(x, y) = 2x + 3y$ , in the region of constraint pictured below.



Notice that if a point satisfies  $y \leq 5$  and  $4x + y \leq 12$  then it also satisfies  $x + 2y \leq 12$ .

$y = 5$  and  $4x + y = 12$  meet at  $\left(\frac{7}{4}, 5\right)$ , and so the maximum value of  $Q(x, y)$  under the constraints is

$$Q\left(\frac{7}{4}, 5\right) = \frac{7}{2} + 15 = \frac{37}{2}.$$