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## Multidimensional Access Structures

COMP3211 Advanced Databases

Dr Nicholas Gibbins - nmg@ecs.soton.ac.uk



#### Overview

- Conventional indexes
- Hash-like
  - grid files, partitioned hashing
- Hierarchical indexes
  - multiple key, kd-trees, quad trees, r-trees, ub-trees
- Bitmap indexes



#### Multidimensional Access Structures

Indexes discussed so far are one-dimensional

- assume a single search key
- require a single linear order for keys (B-trees)
- require that the key be completely known for any lookup (hash tables)



## **Applications**

Geographic information systems

- partial match queries
- range queries
- nearest-neighbour queries

## **Conventional Indexes**



#### Scenario

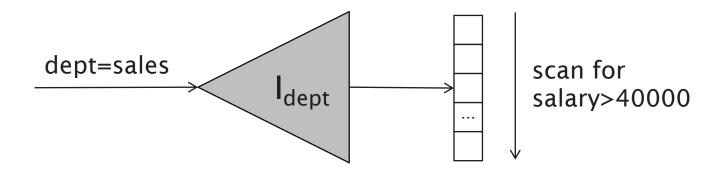
- Personnel database
- EMPLOYEE table with attributes
  - dept
  - salary

• How can we find employees who work in the sales department and have salaries greater than £40,000?



## Approach #1

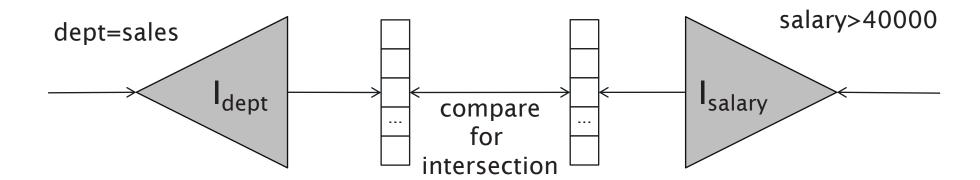
- 1. Get all matching records using an index on one attribute
- 2. Check values of other attribute on those records





## Approach #2

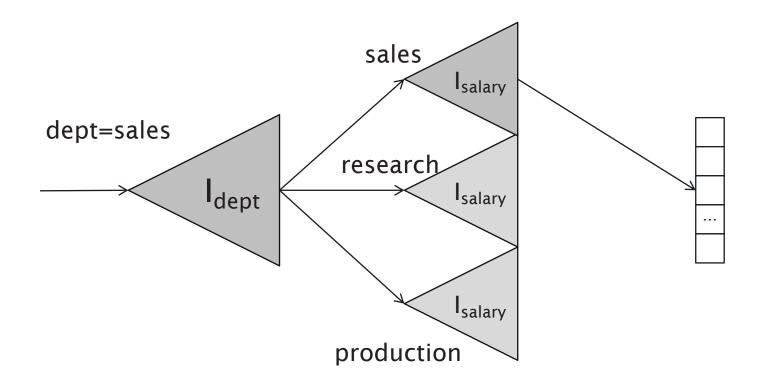
- 1. Use secondary indexes on each attribute to get two sets of record pointers
- 2. Take intersection of sets





## Approach #3

- 1. Use secondary index on one attribute to select suitable index on other attribute
- 2. Get all matching records using selected index





## For which queries is this index good?

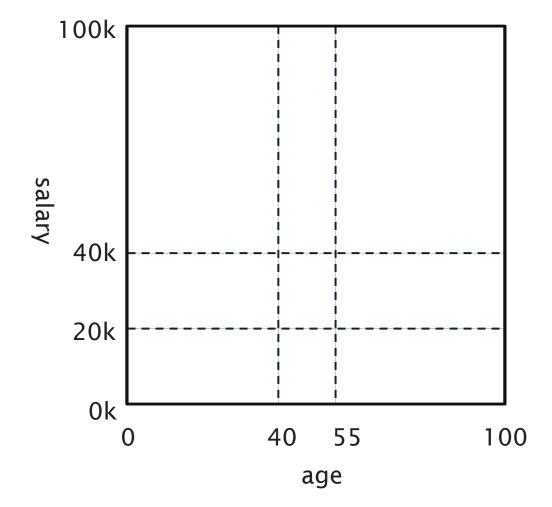
- dept=sales \( \times \) salary=40000
- dept=sales \( \) salary>40000
- dept=sales
- salary = 40000

## **Grid Files**



#### Grid File

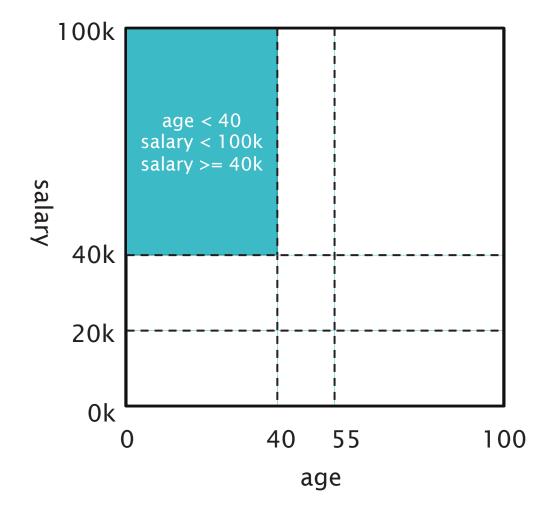
- Partition multi-dimensional space with a grid
- Grid lines partition space into stripes
- Intersections of stripes from different dimensions define regions





#### Grid File

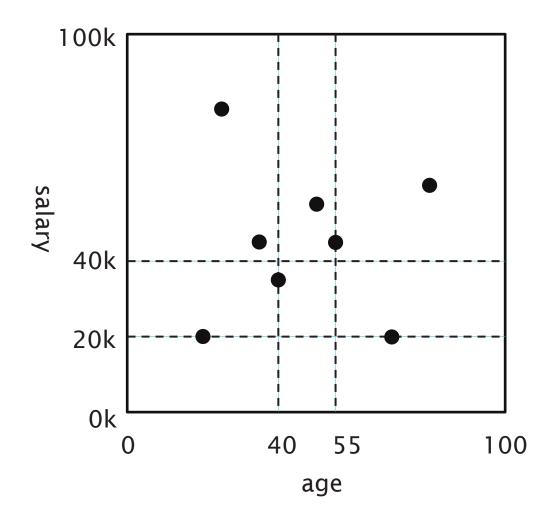
- Partition multi-dimensional space with a grid
- Grid lines partition space into stripes
- Intersections of stripes from different dimensions define regions





#### Grid File

- Each region associated with a pointer to a bucket of record pointers
- Attribute values for record determine region and therefore bucket
- Fixed number of regions overflow blocks used to increase bucket size as necessary
- Can index grid on value ranges





#### Grid files

#### Pro

- Good for multiple-key search
- Supports partial-match, range and nearest-neighbour queries

#### Con

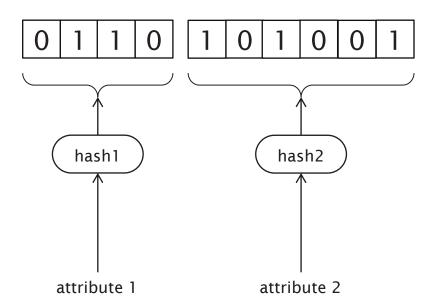
- Space, management overhead (nothing is free)
- Need partitioning ranges that evenly split keys

## Partitioned Hash



#### Partitioned Hash

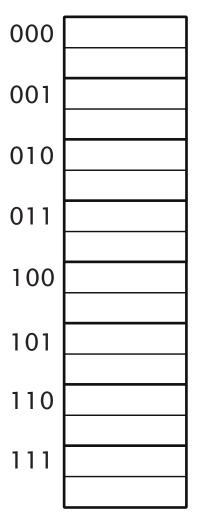
- Hash function takes a list of attribute values as arguments
- Bits of hash value divided between attributes
  - Effectively, a hash function per attribute





# Example

hash1(sales)	=	0	
hash1(research)	=	1	
hash2(10000)	=	00	
hash2(20000)	=	01	
hash2(40000)	=	10	
hash2(100000)	=	11	





#### Insertion

hash1(sales)	=	0
hash1(research)	=	1

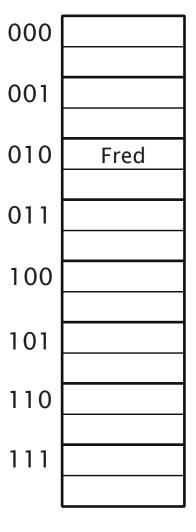
hash2(10000) = 00

hash2(20000) = 01

hash2(40000) = 10

hash2(100000) = 11

Fred works in sales Fred's salary is £40,000





#### Retrieval

hash1(sales)	=	0
hash1(research)	=	1

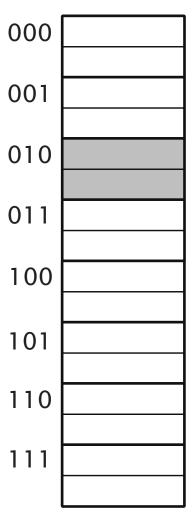
$$hash2(10000) = 00$$

$$hash2(20000) = 01$$

$$hash2(40000) = 10$$

$$hash2(100000) = 11$$

dept=sales \( \salary=40000 \)





#### Retrieval

hash1(sales)	=	0
hash1(research)	=	1

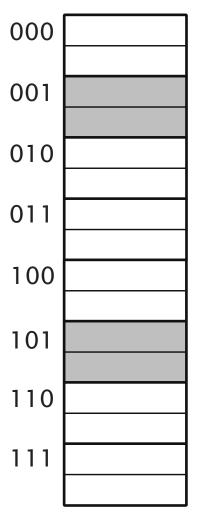
hash2(10000) = 00

hash2(20000) = 01

hash2(40000) = 10

hash2(100000) = 11

salary=20000





#### Retrieval

hash1(sales)	=	0
hash1(research)	=	1

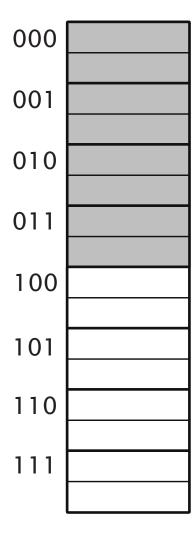
00

$$hash2(20000) = 01$$

$$hash2(40000) = 10$$

$$hash2(100000) = 11$$

dept=sales





#### Partitioned hash

#### Pro

- Good hash function will evenly distribute records between buckets
- Supports partial-match queries

#### Con

• No good for nearest-neighbour or range queries

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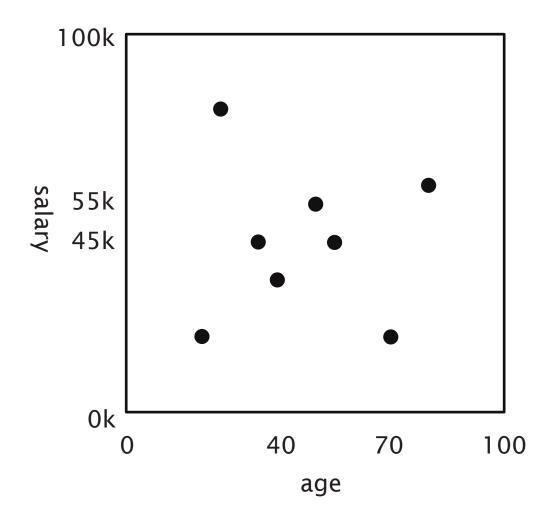
kd-Tree



#### kd-Tree

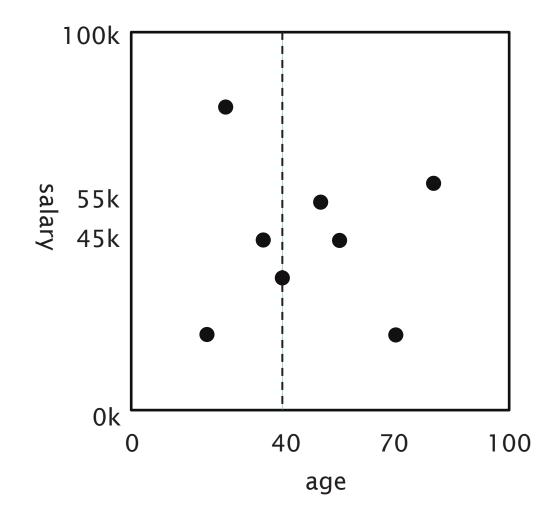
- Multidimensional binary search tree
- Each node splits the k-dimensional space along a hyperplane
- Nodes contain
  - an attribute-value pair
  - a pair of pointers
- All nodes at the same level discriminate for the same attribute
- Levels rotate between attributes of all dimensions



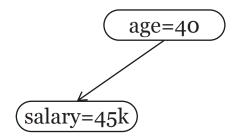


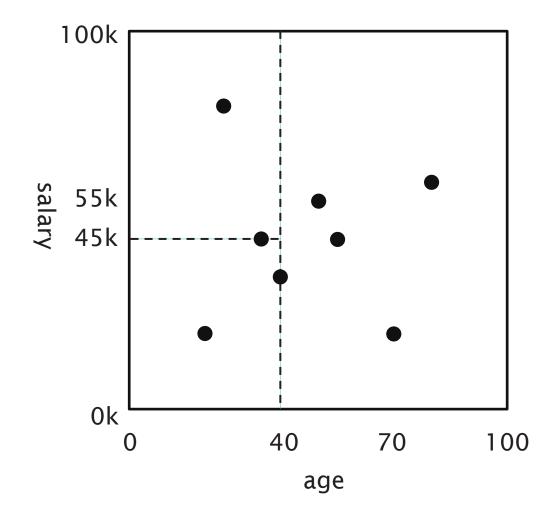


age=40

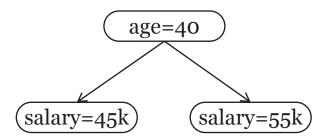


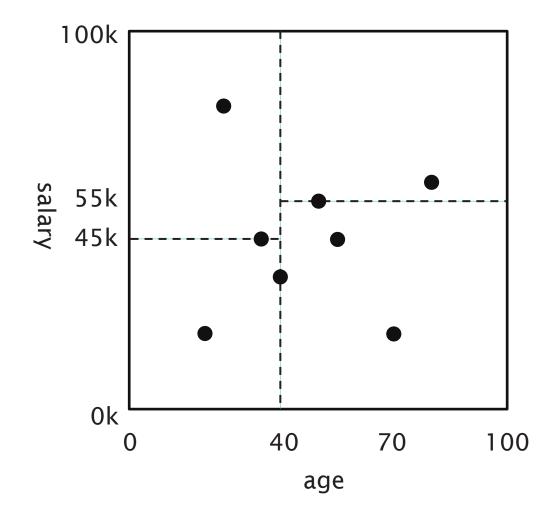




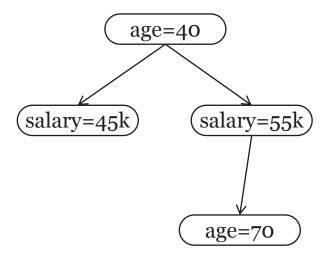


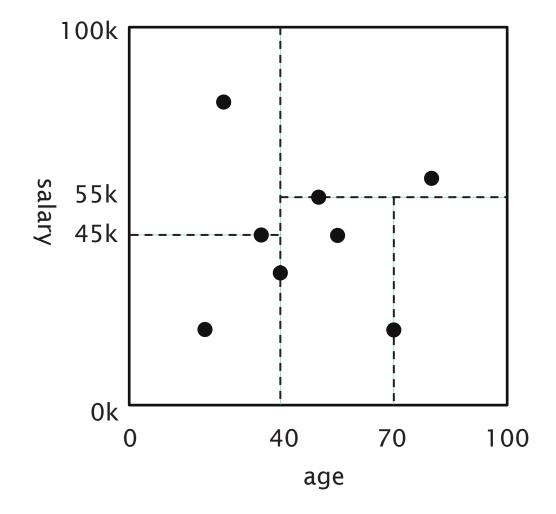




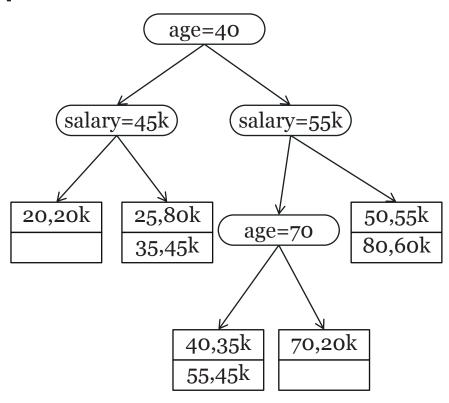


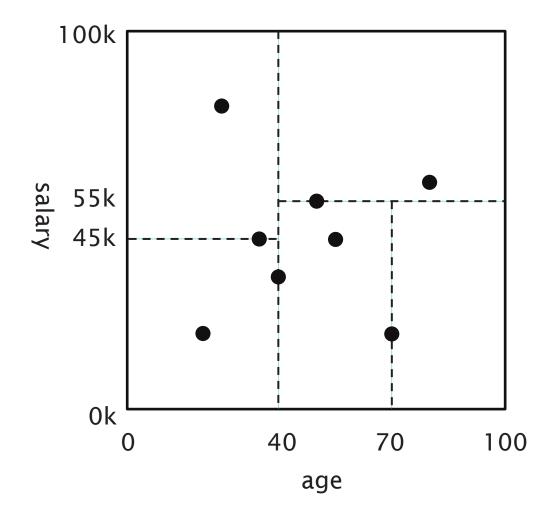














### Partial-Match Queries

- If we know value of attribute, we can choose which branch to explore
- If we don't know value of attribute, must explore both branches



## Adapting kd-Trees to Secondary Storage

Average path length from root to leaf: log<sub>2</sub>n

Disk accesses should be kept as few as possible

#### Two approaches:

- 1. Multiway nodes (split values into n ranges)
- 2. Group nodes in blocks (node plus descendants to a given ply)

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Quad-Tree



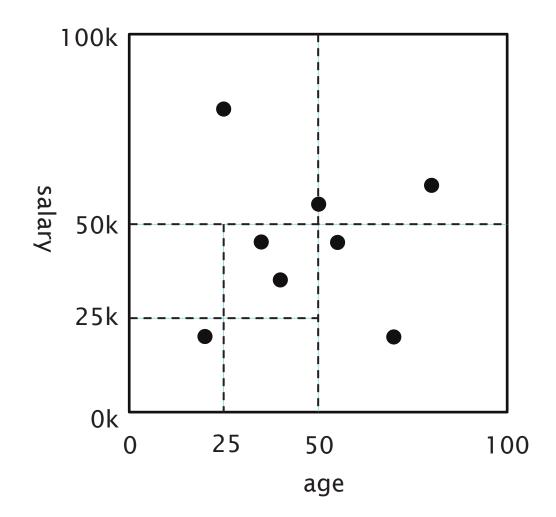
## **Quad-Trees**

#### Two main types:

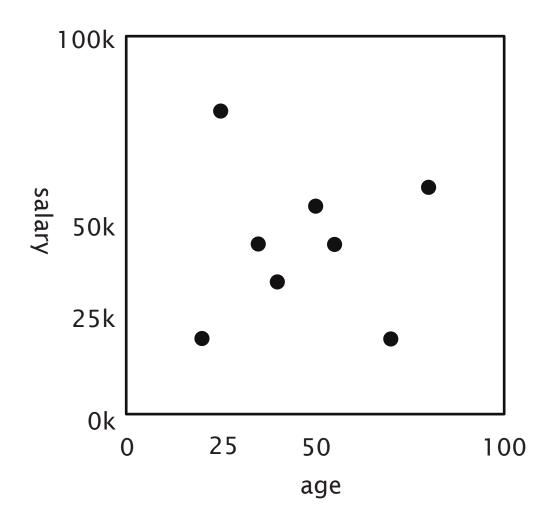
- Region quad-tree
- Point quad-tree



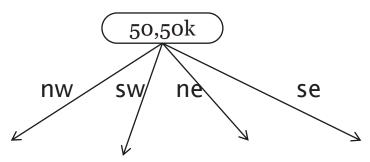
- Each partition divides the space into four equal area sub-regions
  - ne, nw, se, sw
- Split regions if they contain more records than will fit into a block
- Operations similar to those for kd-trees

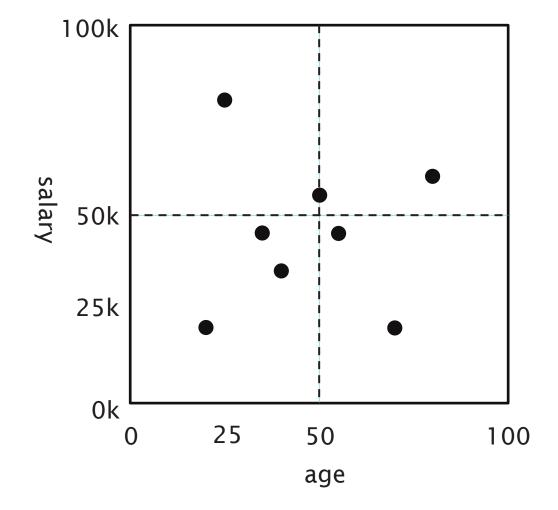




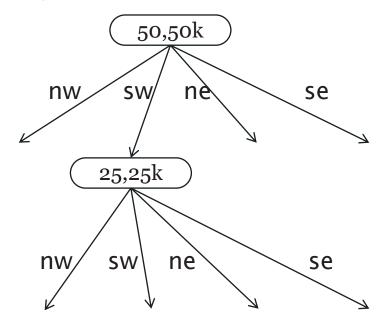


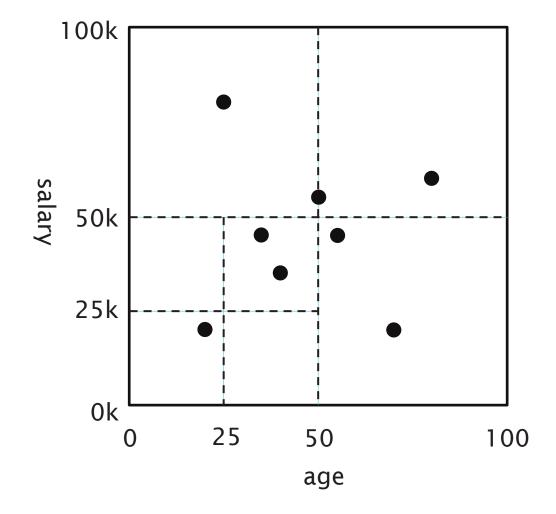




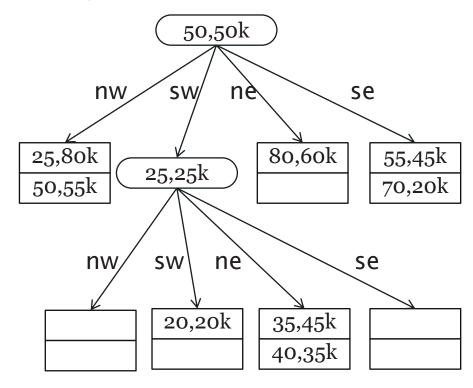


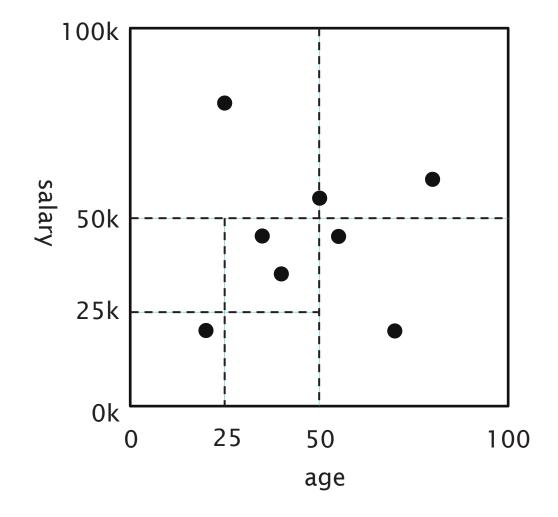






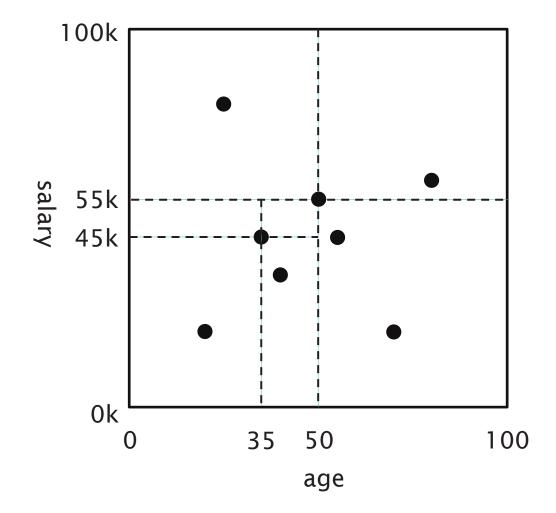




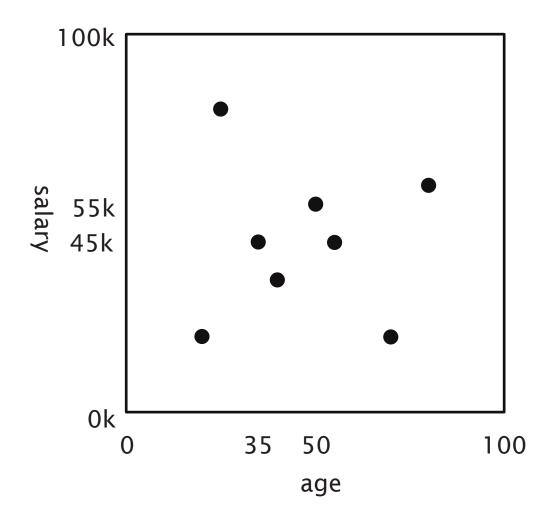




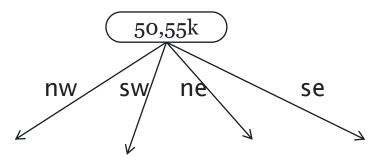
- Partitions are not equal area
  - Split lines centred on data points
  - ne/nw/se/sw sub-regions
- Otherwise, equivalent to region quadtree

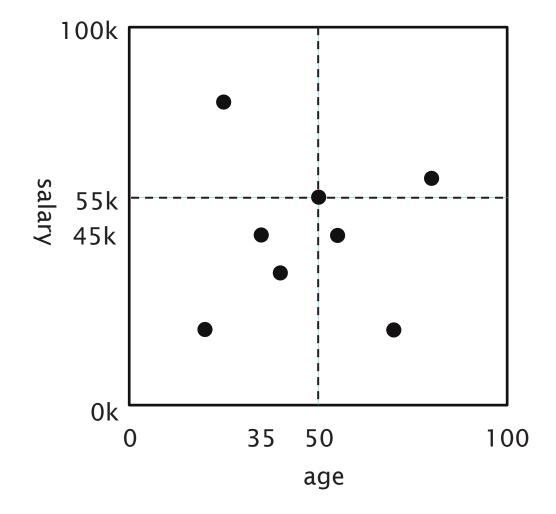




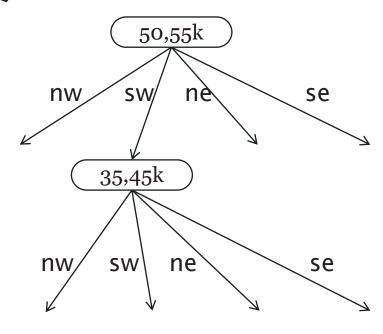


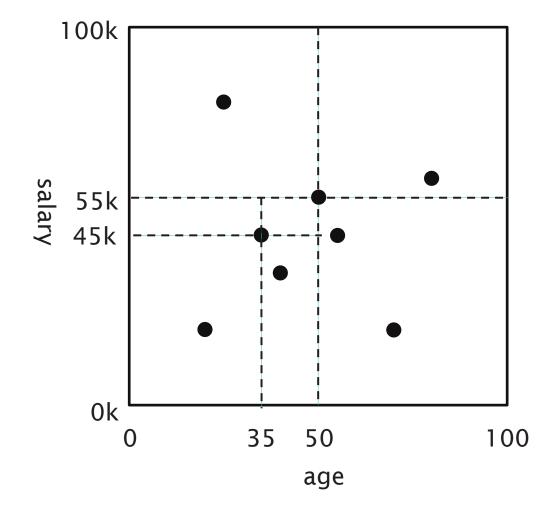




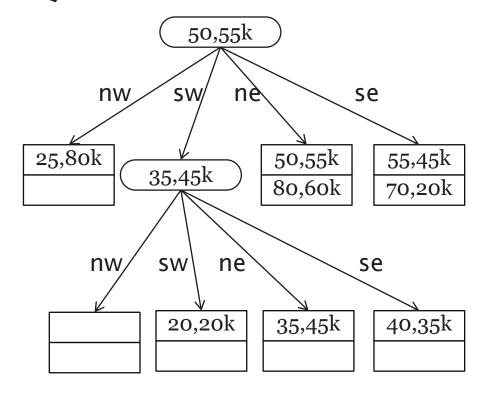


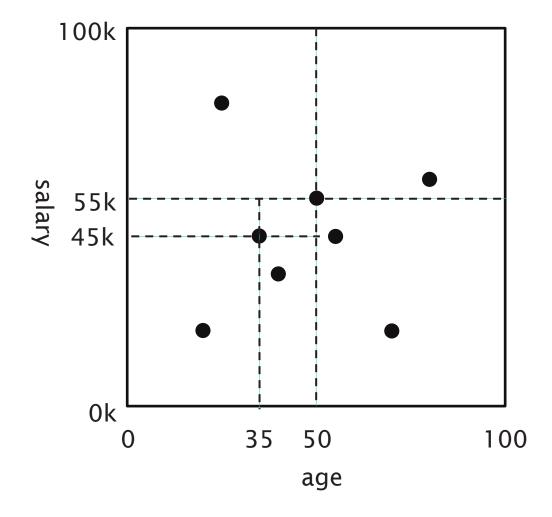






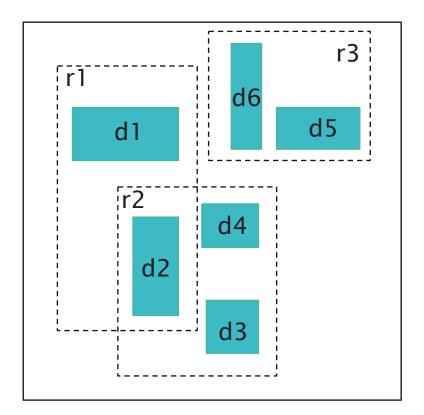






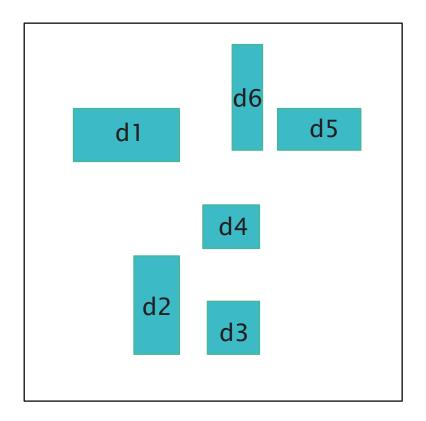


- Used to represent data that consists of k-dimensional data regions
- Internal nodes of tree represent regions that contain data regions
- Regions typically defined as top-right, bottom-left coordinates

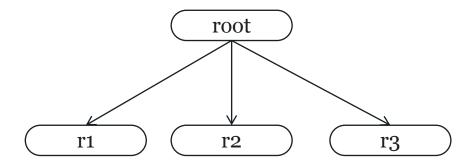


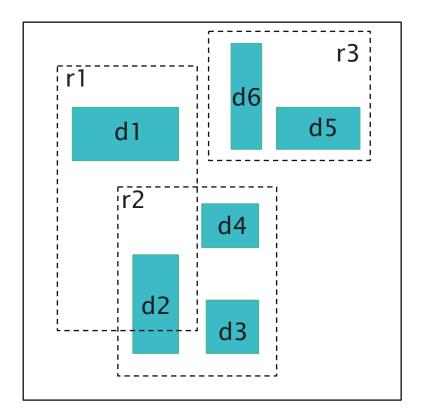


root

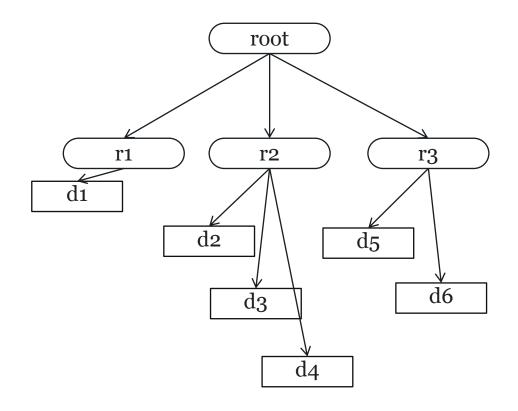


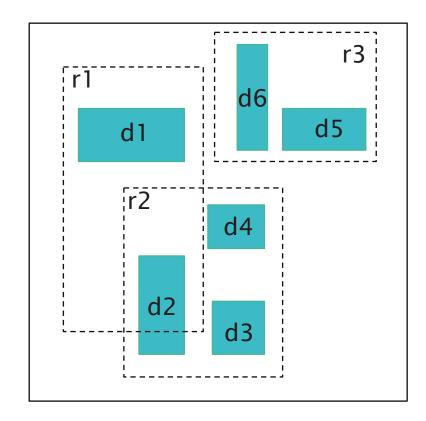












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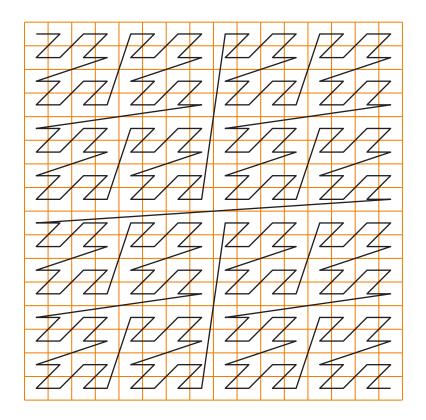
UB-Tree



#### **UB-Tree**

#### Basic approach:

- Map n-dimensional space onto a 1dimensional line using a fractal spacefilling curve
- Partition ranges and index using a B+tree
- When querying, identify regions of n-d space (= segments of 1-d line) that intersect with query rectangle





Map domain of each attribute onto n-bit integer

$$x = x_1x_2$$
  
 $y = y_1y_2$   
 $z$ -index =  $y_1x_1y_2x_2$ 

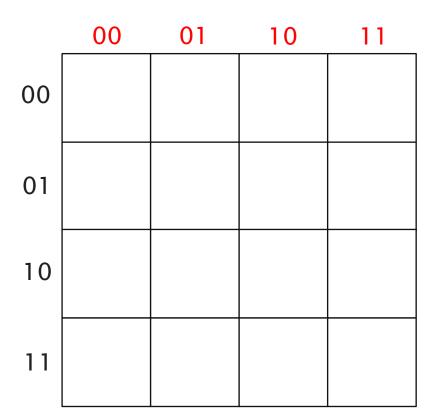


Map domain of each attribute onto n-bit integer

$$X = X_1 X_2$$

$$y = y_1 y_2$$

$$z\text{-index} = y_1x_1y_2x_2$$





Map domain of each attribute onto n-bit integer

$$X = X_1 X_2$$

$$y = y_1 y_2$$

$$z\text{-index} = y_1x_1y_2x_2$$

	00	01	10	11
00	0000	0001	0100	0101
01	0010	0011	0110	0111
10	1000	1001	1100	1101
11	1010	1011	1110	1111

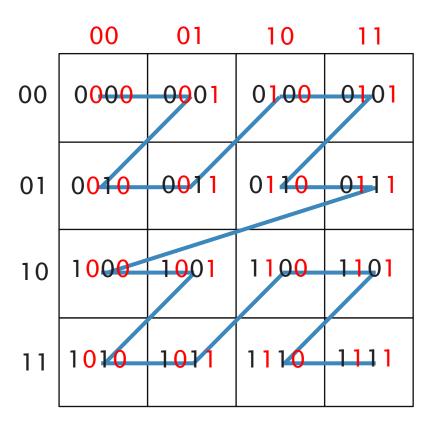


Map domain of each attribute onto n-bit integer

$$X = X_1 X_2$$

$$y = y_1 y_2$$

$$z$$
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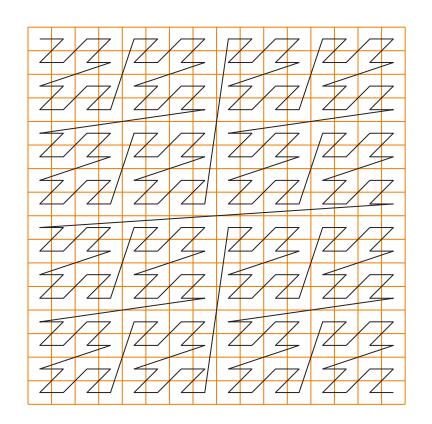
## **Z-Region Partition**

Z-curve partitioned into contiguous ranges (*z-regions*)

 Note that these may not be contiguous regions in the multidimensional space

Z-regions mapped to leaf nodes of a B+tree

 A leaf node contain pointers to records whose attribute value locate them within the associated Z-region







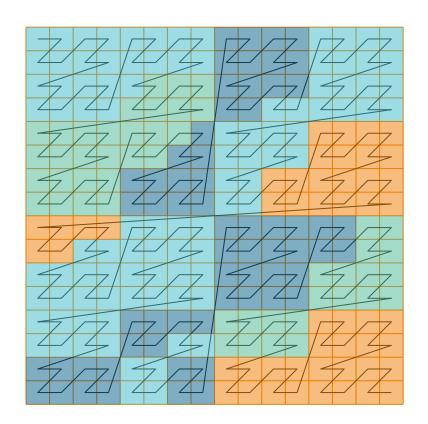
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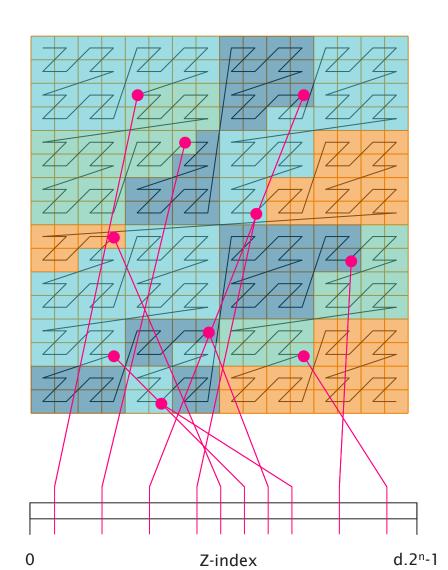
## **Z-Region Partition**

Z-curve partitioned into contiguous ranges (*z-regions*)

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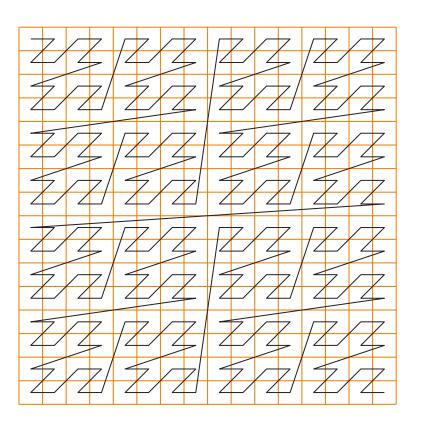
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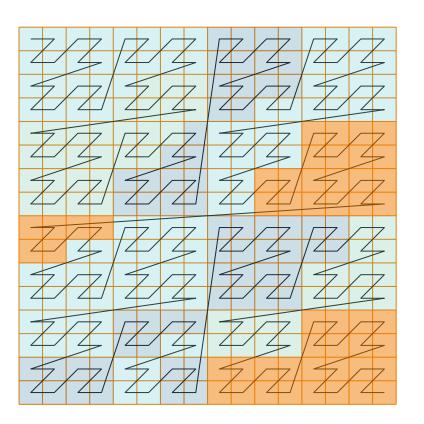


- Multidimensional range query can be considered as a k-dimensional rectangle
- Algorithm identifies z-regions that intersect with the query rectangle



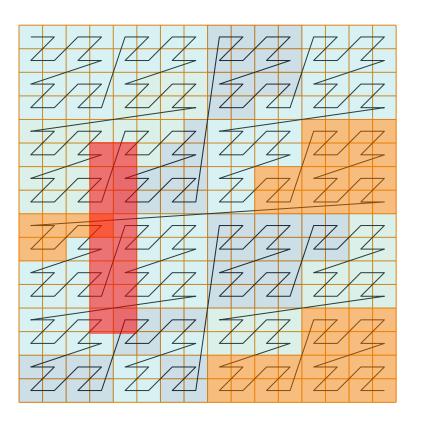


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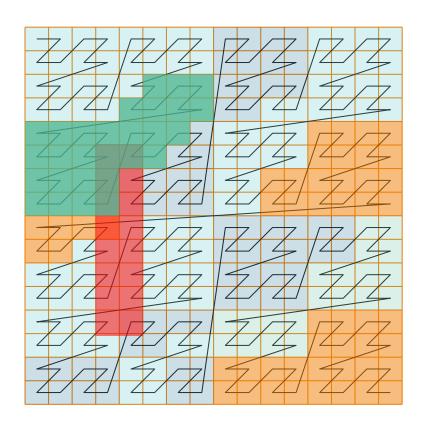


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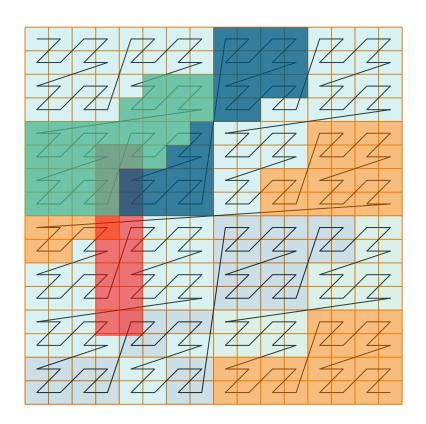


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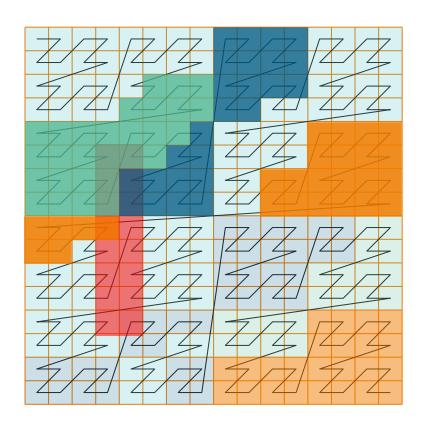


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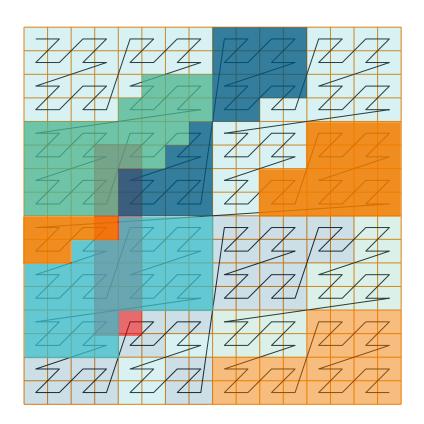


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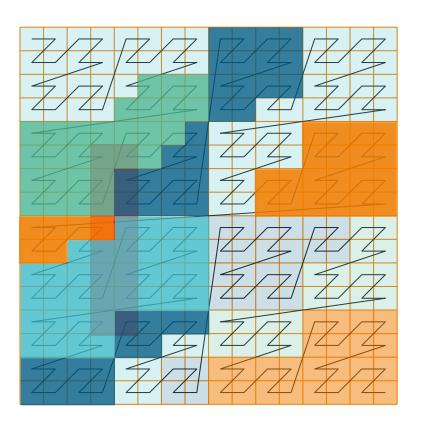


- Multidimensional range query can be considered as a k-dimensional rectangle
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- Multidimensional range query can be considered as a k-dimensional rectangle
- Algorithm identifies z-regions that intersect with the query rectangle



Bitmap Indexes



## Bitmap indexes

Collection of bit-vectors used to index an attribute

- One bit-vector for each unique attribute value
- One bit for each record

Querying index involves combining bit-vectors with bitwise operators (&, |)

• A 1 in the *i*th position indicates that record *i* is a match



# Example

An online homeware vendor sells products p1...p10

- Products p3 and p5 cost £100
- Product p1 costs £200
- Products p2, p7 and p10 cost £300
- Products p4, p6, p8 and p9 cost £400
- Products p1, p4, p5 and p9 are designed for lounges
- Products p5 and p7 are designed for dining rooms
- Products p3, p5, p6 and p10 are designed for kitchens



	<b>p1</b>	p2	р3	p4	<b>p</b> 5	р6	р7	р8	р9	p10
£100	0	0	1	0	1	0	0	0	0	0
£200	1	0	0	0	0	0	0	0	0	0
£300	0	1	0	0	0	0	1	0	0	1
£400	0	0	0	1	0	1	0	1	1	0
Lounge	1	0	0	1	1	0	0	0	1	0
Dining	0	0	0	0	1	0	1	0	0	0
Kitchen	0	0	1	0	1	1	0	0	0	1



	<b>p</b> 1	p2	р3	р4	р5	р6	р7	p8	р9	p10
£100	0	0	1	0	1	0	0	0	0	0
£200	1	0	0	0	0	0	0	0	0	0
£300	0	1	0	0	0	0	1	0	0	1
£400	0	0	0	1	0	1	0	1	1	0
Lounge	1	0	0	1	1	0	0	0	1	0
Dining	0	0	0	0	1	0	1	0	0	0
Kitchen	0	0	1	0	1	1	0	0	0	1

 $price=£300 \land room=kitchen$ 



	<b>p</b> 1	p2	р3	p4	р5	р6	р7	p8	р9	p10
£100	0	0	1	0	1	0	0	0	0	0
£200	1	0	0	0	0	0	0	0	0	0
£300	0	1	0	0	0	0	1	0	0	1
£400	0	0	0	1	0	1	0	1	1	0
Lounge	1	0	0	1	1	0	0	0	1	0
Dining	0	0	0	0	1	0	1	0	0	0
Kitchen	0	0	1	0	1	1	0	0	0	1

 $price=£300 \land room=kitchen$ 

0100001001 & 0010110001 = 000000001



	<b>p</b> 1	p2	р3	p4	р5	р6	р7	p8	р9	p10
£100	0	0	1	0	1	0	0	0	0	0
£200	1	0	0	0	0	0	0	0	0	0
£300	0	1	0	0	0	0	1	0	0	1
£400	0	0	0	1	0	1	0	1	1	0
Lounge	1	0	0	1	1	0	0	0	1	0
Dining	0	0	0	0	1	0	1	0	0	0
Kitchen	0	0	1	0	1	1	0	0	0	1

 $price=£300 \land room=kitchen$ 

0100001001 & 0010110001 = 0000000001

p10 is matching product



## Compression

- Bit-vectors are typically sparse, with few 1 bits
  - Large amount of wasted space
  - Run-length encoding of bit-vectors to reduce stored size
- Bitwise operators must be applied to original bit-vectors
  - Can decode RLE bit-vectors one run at a time



# Bitmap indexes

#### Pro

• Efficient answering of partial-match queries

#### Con

- Requires fixed record numbers
- Changes to data file require changes to bitmap index

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Next Lecture: Relational Algebra