

Partial Differentiation
Limits

Question

Evaluate the given limit. If the limit does not exist, explain why.

$$\lim_{(x,y) \rightarrow (0,0)} \frac{y^3}{x^2 + y^2}$$

Answer

$$\left| \frac{y^3}{x^2 + y^2} \right| \leq \frac{y^2}{x^2 + y^2} |y| \leq |y| \rightarrow 0$$

as $(x, y) \rightarrow (0, 0)$.

$$\Rightarrow \lim_{(x,y) \rightarrow (0,0)} \frac{y^3}{x^2 + y^2} = 0$$