$\begin{array}{c} {\rm Vector\ Fields} \\ {\it Scalar\ and\ Vector\ Fields} \end{array}$

Question

Sketch the following plane vector field and determine its field lines.

$$\underline{F}(x,y) = \nabla(x^2 - y)$$

Answer

The field lines satisfy $\frac{dx}{2x} = \frac{dy}{-1}$. They are the curves $y = -\frac{1}{2} \ln x + C$.

